

Original Article

A combination Technique based on Polynomial Method and look-up Table for Linearity Digital Pre-distortion in Power Amplifiers

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ABSTRACT

In this article, a new technique is proposed for linearity digital pre-distortion in power amplifiers for Orthogonal Frequency Division Multiplexing (OFDM) systems. For this purpose, a combination technique comprising look-up table (LUT) method and polynomial method is employed. For the Linear power amplifiers of the least mean square (LMS) method is a adaptive method, as possible a few hardware in implementation used and to have a fast response capability. Coefficients of look-up table are estimated by LMS method as a forward program with the least error amount in order to estimate modulator output of OFDM. In addition, designing of several radio frequency (RF) power amplifiers and their linearization unit in elimination of non-linear distortions of these amplifiers by linearity unit, and yet various realistic involved phenomena in base-band pre-distortion system design, are studied. Measures such as Adjacent Channel Power Ratio (ACPR) were adopted for the purpose of linearization measurement and comparison. The obtained results of the proposed technique are presented both by look-up table and frequency spectrum of output signal. The results also indicate appropriate performance of the proposed technique. Simulations were carried out on ADS software, while final signal output was extracted by MATLAB.

Keywords: Digital Pre-distortion, Power amplifier, Linearization, OFDM, Look-up table method, Polynomial method.

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INTRODUCTION

In recent years, many attentions have been paid on high spectrum performance by many digital radio system designers. In order to increase data speed per frequency band, systems with multi-level modulations, including M-QAM, OFDM, and etc., have been extended. OFDM method is a very proper technique in high rate sending and optimum band utilization, enabling it to be robust against multi-path distortions. It is, thus, utilized in many broadcasting stations (Birafane *et al.*, 2010). However, the main problem of this method is the peak-to-average power ratio signal to mean power signal, which results along with non-linear

characteristics of power amplifier in output distortion. Furthermore, due to wideness of signal band of OFDM, non-linear characteristics of power amplifier AM/AM/ and AM/PM are made frequency dependent (memory) (Nader *et al.*, 2011). So far, various techniques have been proposed to overcome this problem. As such, design improvement methods, the peak to average power ratio decrease methods, and linearization methods applied on amplifier. Linearization methods are: power storage method, feedback method with modulation and push, Polar and Cartesian loop (Boo *et al.*, 2011), linear amplification with non-linear component (LINC) method (Gilabert *et al.*, 2011), forward method, pre-distortion method. Pre-distortion method is the simplest linearization method in terms of concept. In this method, a distortion characteristic is constructed. This is precisely the supplement of distortion characteristics of RF power amplifier which are cascaded in a way that the overall input-output distortion is negligible (Lee *et al.*, 2010). Pre-distortion methods consist of analog and digital pre-distortion. Digital pre-distortion (DPD) are: (1) look-up table and (2) a polynomial function expressed by polar coordinates (amplitude and phase) or Cartesian coordinates (Chung *et al.*, 2010). So far, various applications of these methods and/or a combination of them are presented, which will be mentioned in the following.

In (Park *et al.*, 2000), a digital pre-distortion technique was employed for linearization and efficiency improvement of high-voltage Class AB power amplifier for ultrasound transmitters. In (Gilabert *et al.*, 2012), a Slow Envelope Dependent digital pre-distortion (SED-DPD) was proposed capable of compensating non-linear distortion and memory effects. In (Ai *et al.*, 2008; Mrabet *et al.*, 2012), a new polynomial formulation based on digital pre-distortion was presented. This formula reduces hardware resources, memory and logic, required for implementation while holding enough precise. In addition, calibration of transmitter and receiver minimizes its distortion. In (Kardaras *et al.*, 2010), a simple method was presented using a digital pre-distortion of polynomial in frequency domain of IF which can be completely implemented in software without requiring any hardware. In (Liu *et al.*, 2012), a 2-D modified memory polynomial method was proposed in order to compensate non-linear distortion in simultaneous dual-band transmitters. In (Aladr *et al.*, 2012), a novel pre-distortion model using orthogonal proposal was proposed which is composed of a ZERNIKE polynomial. ZERNIKE polynomial is a sequence of polynomials perpendicular to unit disc. In (Younes *et al.*, 2012), a new and precise model with less complexity was that this model utilizes a parallel combination of look up table (LUT) and a memory polynomial MP-EMP, called PLUME. In (Hussein *et al.*, 2012), a 2-D MSP model was presented for digital pre-distortion. This model indicates comparative performance using conventional polynomial models such as general memory polynomial (GMP) by significantly less parameters. In Durney and Sala (2012) a relatively heuristic method was proposed using capability distribution function (CDF) of power amplifier input and output. This method could properly compensate non-linear effect of AM/AM conversion. In (Li *et al.*, 2011), two algorithms were analyzed. In addition, a combined algorithm comprising pre-distortion algorithm of look-up table and memory polynomial was introduced. In (Hammi *et al.*, 2009), a new model named TNTB was proposed. This model comprises of three models of PTNTB, RTNTB, and FTNTB. These proposed models obtain a more general model of non-linear distortion and memory effects compared to the previously presented models.

In this paper, a method by combining of look-up table and polynomial methods will be proposed in which look-up table coefficients is estimated by LMS by a forward program with the least error rate. This not only leads to increased convergence of algorithm, but also results in less hardware usage in implementation, making it less computationally complex and fast response capability. Furthermore, OFDM signals were used for linearization purposes. Operating frequency is close to 950MHz and OFDM 64-QAM signal is used for data rate increase. In the following, description of polynomial method, look-up table method, proposed algorithm, and simulation results will be addressed. Conclusion and references are the final parts.

Overview on Digital Pre-distortion (DPD) Models

Adaptive Digital Pre-distortion for linearity Power Amplifier (PF)

Linearity of pre-distortion as shown in Fig. 1 can be utilized in linearity more than one broad bandwidth. This can be obtained through signal pre-distortion before amplification by reverse characteristics of pre-distortion imposed on power amplifier. Thus, power amplifier (PA) output is a linearization function of a pre-distorter input (eq.1):

$$y(t) = f(x(t)) \tag{1}$$

$$y(t) = f [g(w(t))] = k \cdot w(t)$$

Adaptive pre-distortion characteristic is to minimize mean error square between PA output and a small version of base band signal using LMS algorithm. This system's simulation indicates that this system is capable of reducing 40 dB in ACPR, reducing 3rd and 5th inter-modulation distortion (IMD) (Muhonen *et al.*, 2000 and Boo *et al.*, 2009).

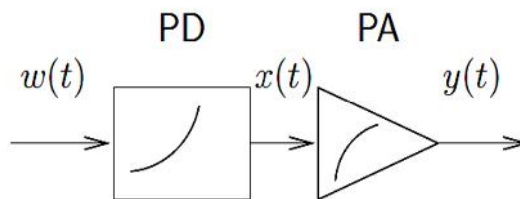


Fig. 1: Base Diagram for Pre-distortion System

Digital Pre-distortion Technique of high-voltage Power Amplifier using Look-up Table

Fig. 2 shows DPD block diagram comprising a DAC, an ADC and one FPGA in which DPD is programmed and delay and memory coordination block diagrams of LUT are constructed. At the instant $t=t_0$, FPGA sends an ideal sine signal $U(t)$. The output of this non-linear system is constant time extendable by Taylor expansion of $U(t)$ in which A_1, A_2 , and A_3 are first, second, and third gain of non-linear amplifier (Gao and gui, 2012). (eq. 2):

$$o(t) = A_1 \cdot u(t) + A_2 \cdot u(t)^2 + A_3 \cdot u(t)^3 + \dots \tag{2}$$

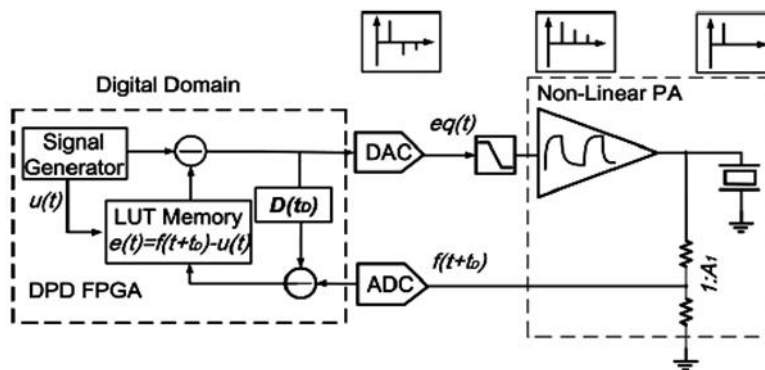


Fig. 2: Block diagram of DPD System of Look-up Table

Digital pre-distortion based on look-up table method for ultrasonic transmitters, DPD scheme perform in the digital amplitude And Implementation of this method is divided into calibration and evaluation phases (Fig. 3). In calibration step, using least mean square of error, system searches optimal error and stores the error in look up table memory. In evaluation phase, equalized input signal phase is added to the input. Then, the equalized input is converted to analog signal using DAC and transmitted to AB class for elimination of non-linear characteristic. In this algorithm, both signals work with constant amplitude (Chung *et al.*, 2010; Gao and gui, 2012).

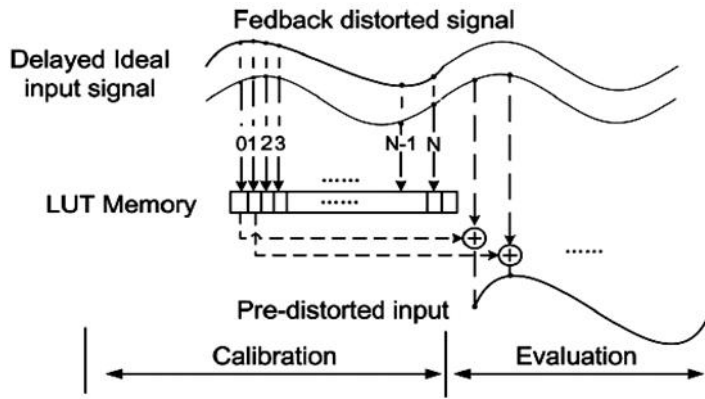


Fig. 3: Pre-distortion System Effect on Harmonics and Calibration and Evaluation Phases in LUT Method

Digital Pre-distortion (DPD) System by Polynomial Method

Polynomial digital pre-distortion system is shown in Fig.4 and Fig.5. System input will be modulation signal quadrature amplitude modulation (QAM). At first, base-band signal will have bandwidth of 150 kHz. This signal is distorted to a modulated analog signal which was prior introduced and amplified into a digital signal via a polynomial pre-distorter. Base-band signal is converted into polar coordinates in order to distort independently into AM-AM and AM-PM. Power amplifier (PA) output is sampled using an analog-digital converter (ADC), and then it is utilized to update pre-distortion in relation to pre-distorter input. Least mean square (LMS) is used to adjust polynomial coefficients. Thus, error mean square of each cycle is computed and compared with previous cycle's mean square error (MSE) using LMS algorithm (Ai *et al.*, 2008; Mrabet *et al.*, 2012; Gao and gui, 2012).

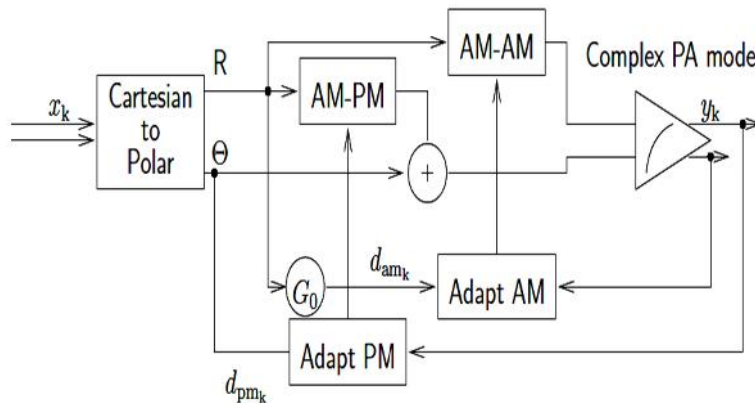


Fig. 4: System diagram of polynomial method for simultaneous improvement of distortion amplitude and phase

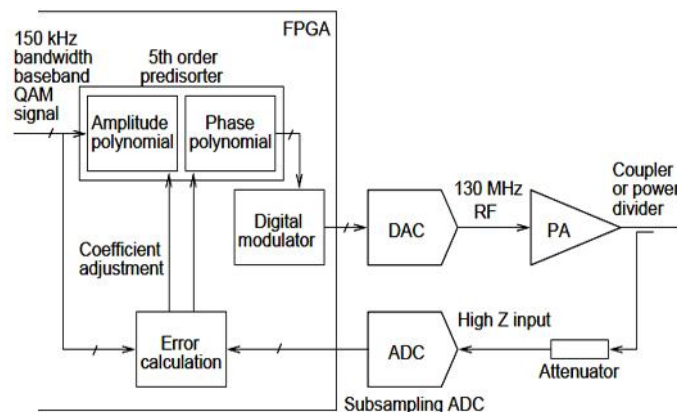


Fig. 5: System diagram of polynomial method Pre-distortion and Implementation Procedure

Proposed Algorithm for Linearity of power Amplifier

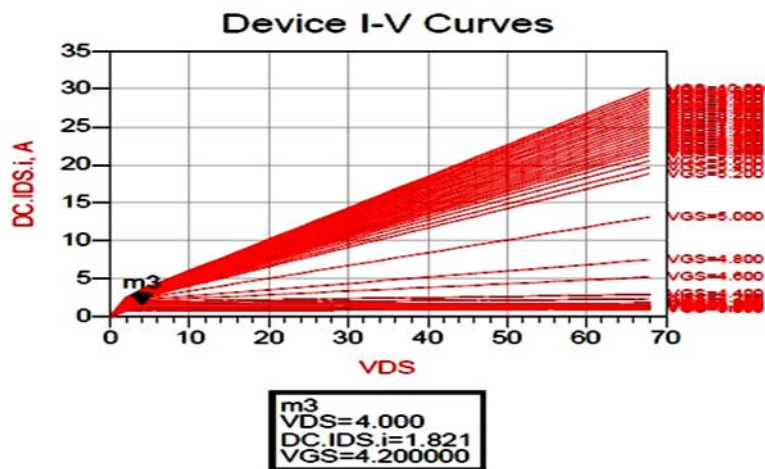
RF power amplifiers linearization in order to eliminate negative effects of non-linear distortions resulting from these amplifiers is one of the modern electronic and communication engineering issues. In this paper, a novel hybrid method comprising polynomial method and Look-up table method is used in order to linearization pre-distortion in power amplifiers based on the proposed adaptive LMS algorithm. In this method, in order to estimate output modulator of OFDM system, coefficients related to look-up table are estimated by LMS method as a forward programming with the least rate error. In addition, OFDM signals are used for linearity purpose. Operating frequency is close to 950 MHz and OFDM 64-QAM signal is used for data rate increase. In summary, the hybrid look-up table and polynomial are given as: 1) Before data storage related to input signal distortion, data is improved by a polynomial algorithm in polynomial block, then it is stored for input signal distortion in LUT memory. 2) Signal phase is used as a memory key for data revision. 3) The attenuated signal by polynomial algorithm is used in the related block for generation of reversed distortion of unwanted harmonics. 4) It should be noted that, high memory is required in the absence of polynomial algorithm. In addition, application of this algorithm leads to reduced signal for updating look-up table. In fact, simultaneous application of look-up table and polynomial algorithm results in reduced time to reach optimum solution.

SIMULATIONS AND DISCUSSIONS

Various steps should be considered in design of a power amplifier. These steps are: DC simulation to find system operating point, small-signal simulation to achieve S-parameters values and estimate stability model in corresponding frequency and bias range, adaptive networks of input and output impedance using simulation test Load-pull to find the best solution. Finally, overall system should be optimized in order to have output power, gain, and efficiency.

DC Analysis

Prior to constructing of circuit, maximum permissible DC power loss should be determined. For this, maximum power loss is obtained by transistor values and I-V characteristic. $P_{d,max}$ which is maximum permissible DC power loss, limits bias level selection to the secure region for transistor and avoids of self-thermal damages. Results related to I-V curve in DC analysis is shown in Fig.6, Considering $P_{d,max}$, and V_{ds} , the following operating point is obtained: $V_{ds}=28V$, $V_{gs}=5 V$, $I_{ds}=2.2 A$.



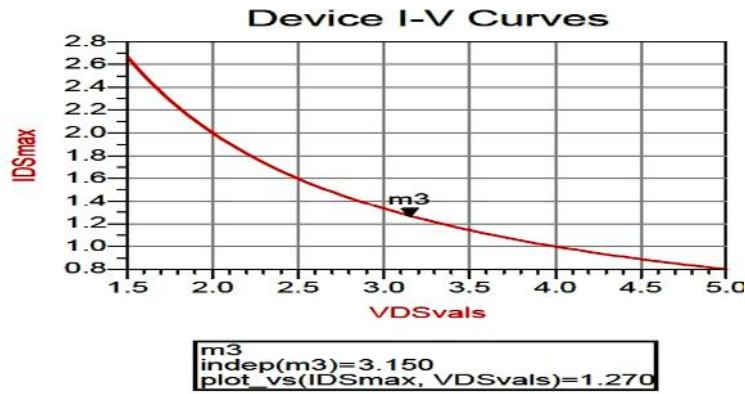


Fig. 6: I-V Curve and Transistor Secure Region

Load-pull Simulation

The aim of Load-pull test is to find optimum load value maximizing output power and efficiency. Thus, various values are dedicated to load impedance in order to optimize this value. Then, adaptive output circuit for optimum impedance load is designed. Before implementation of simulation, several parameters are given as follows:

$RF_{freq}=950MHz$, $V_{high}=28V$, $V_{low}=5V$, $Gain_Comp=1\text{ dB}$, $P=30dBm$, $Z_0=50$.

These values result in optimum load in 1dB compactness. Load-pull simulation results are shown in Fig.7 Optimal load is $Z_l=7.161+j2.480$, resulting in optimum output power of 35.85dB and PAE=2.31%. Load-pull is one of the best methods for output power calculation.

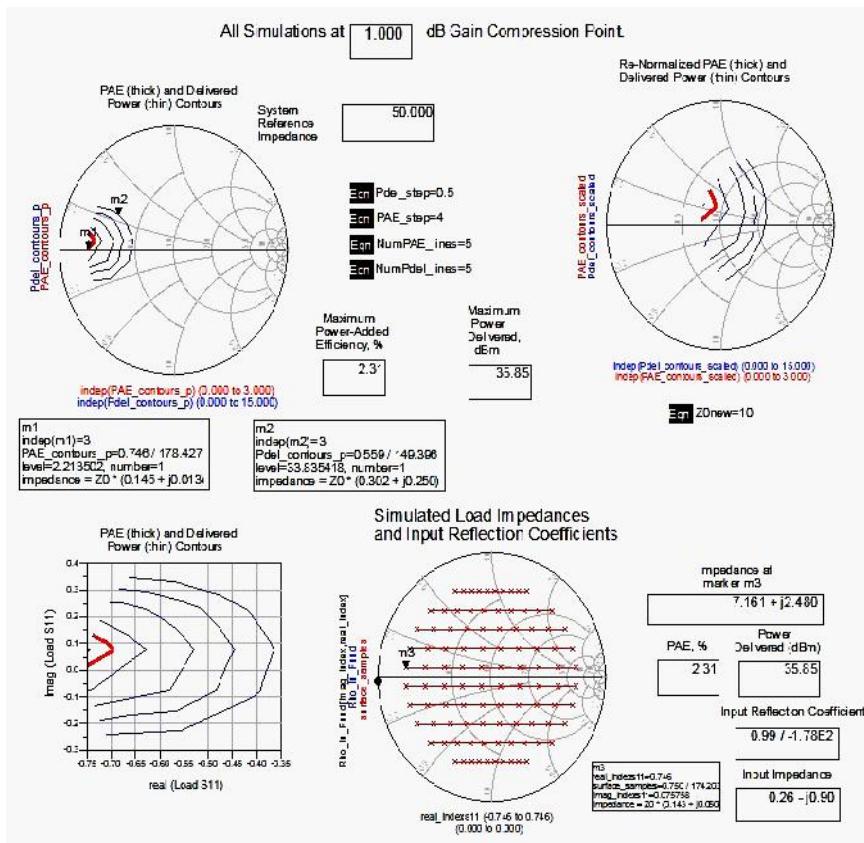


Fig. 7: Load-pull Simulation Results

Designing of Final Circuit of Amplifier

The final designed circuit is shown in Fig. 8. In order to design amplifier, first, to prevent memory effects a passive bias circuit, consisting of inductors and capacitors, is used which is selected by operating frequency 950 MHz.

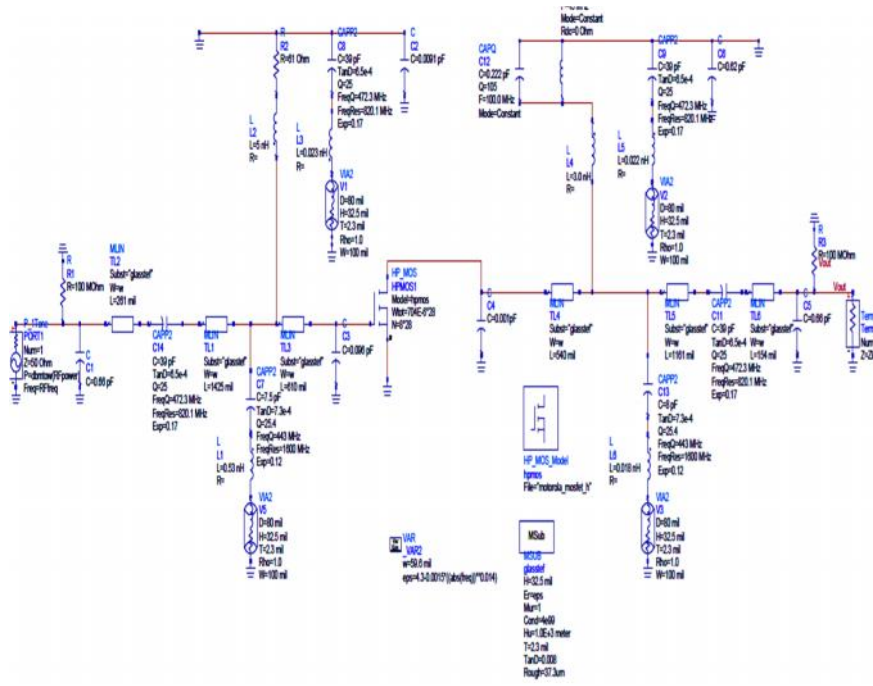


Fig. 8: Schematic of Final Circuit Amplifier

Considering designed final circuit and harmonic test of circuit, the following results are obtained Fig. 9. High the peak to average power ratio (PAPR), is one of the main challenges in OFDM systems, affecting system performance. In most of the reported literature, this problem is considered as the most important problems in OFDM. In this paper, high PAPR problem is resolved by a combination of the proposed methods.

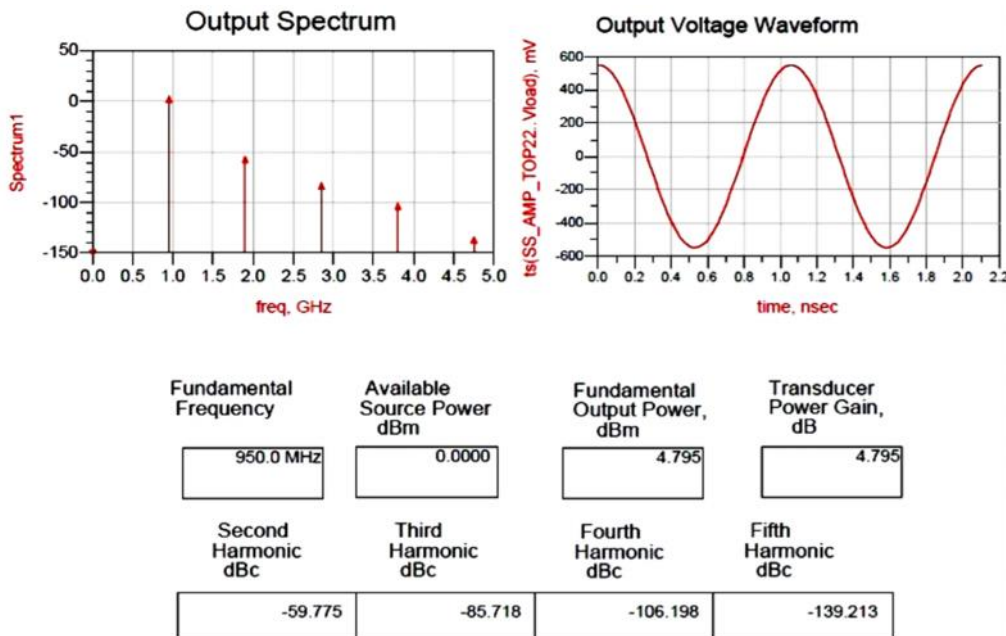


Fig. 9: Harmonic Test Results of Amplifier

Generation of OFDM reference Signal using IEEE Standard

Simulation of modulated OFDM signal with IEEE 802.11a standard is illustrated in Fig. 10. Simulation of this simulation is depicted in Fig. 11.

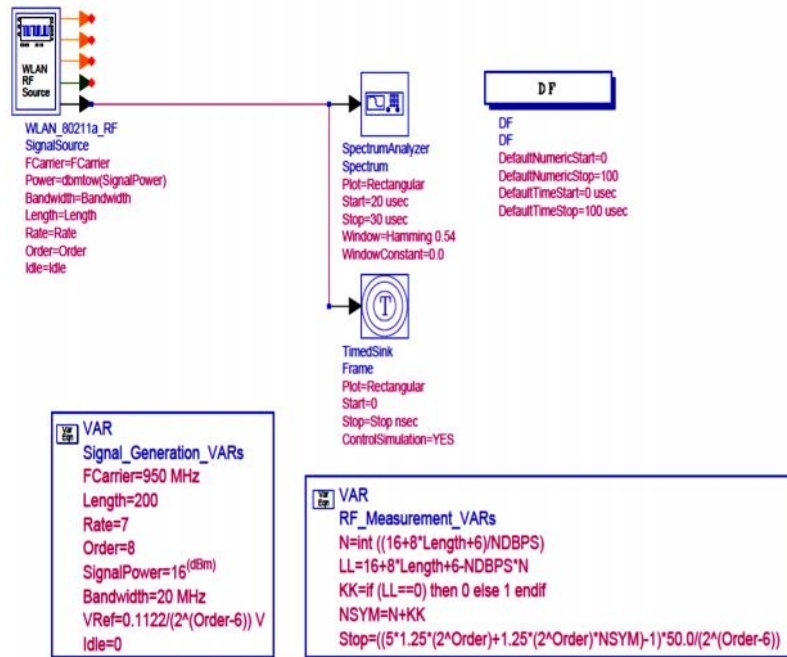


Fig. 11: Simulation of OFDM Signal IEEE standard

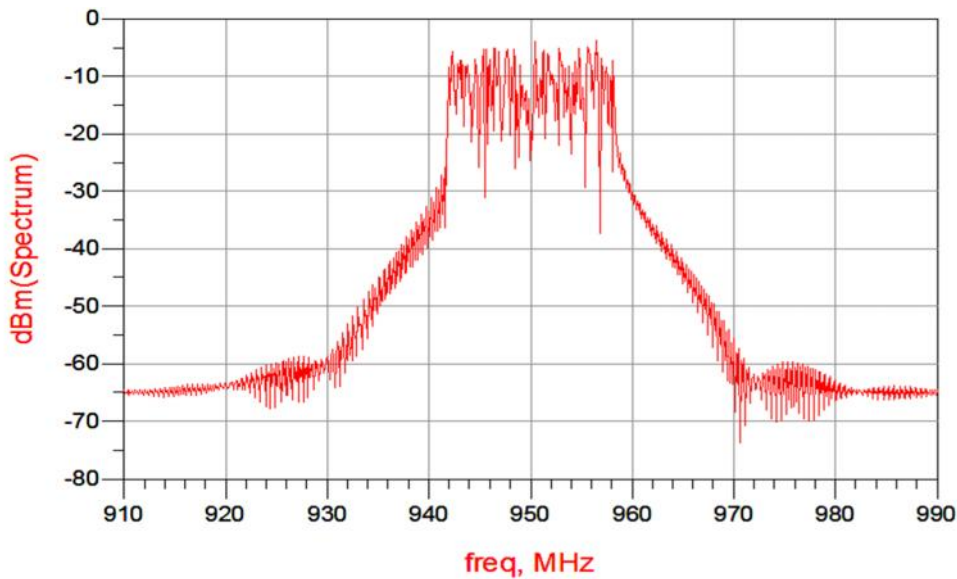


Fig. 12: Simulation of Modulated OFDM Signal

Power Amplifier Effect on OFMD Signal

In this section, non-linear effect of amplifier on parameters such as CCDF and RF output spectrum are examined using Agilent EESOF ADS. IEEE 802.11a standard uses OFDM-64-QAM signal for increasing data rate its push with regard to man line of power signal has large variations. In order to depict these changes, PAPR measure was proposed. Possibility distribution PAPR is usually expressed as CCDF signal. CCDF is more common than CDF and is obtained by subtraction of CDF (possibility supplement CDF). CCDF diagram is shown in Fig. 13. For this signal in the absence of amplifier and in the presence of amplifier with saving power of 5dB. Horizontal axis indicates power signal higher than power signal in terms of dB, while vertical axis demonstrates possibility percentage.

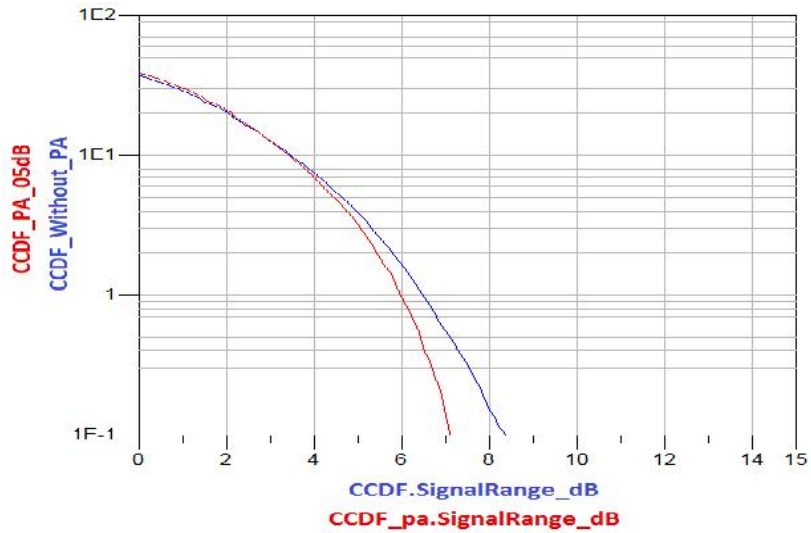


Fig. 13: CCDF for two cases in the absence of amplifier and in the presence of with saving power 5dB

Spectrum of Output Radio frequency Signal (RF)

Output spectrum of modulator and amplifier without digital pre-distortion is shown in Fig. 14 and Fig. 15.

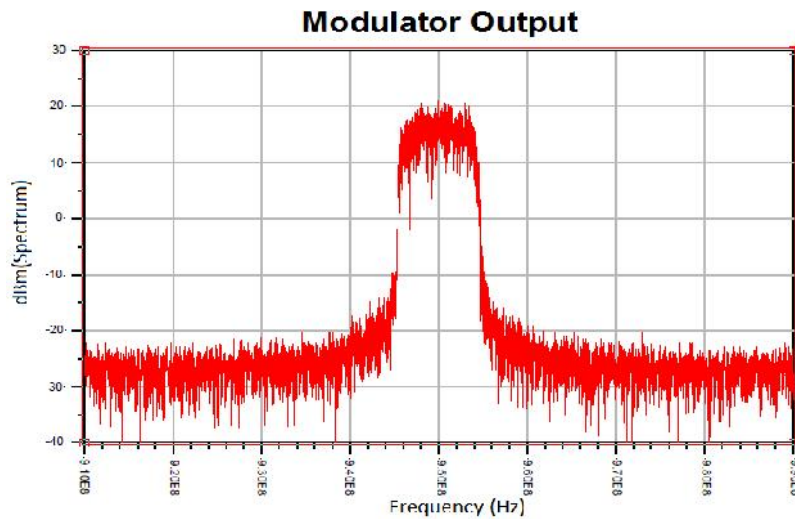


Fig.14: Modulator Output without digital-Pre-distortion

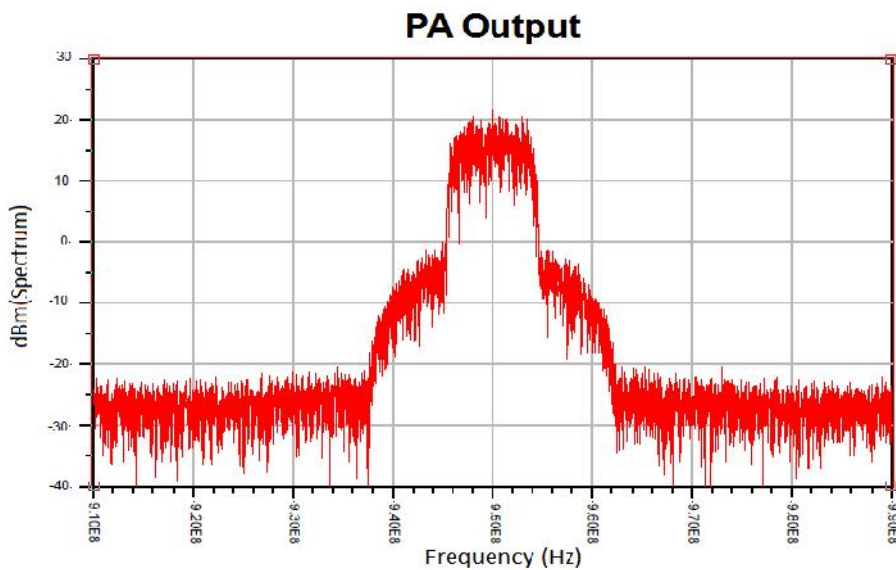


Fig.15: Amplifier Output without digital-Pre-distortion

Look-up Tabled based on Proposal Method

In this method, transmitted signal has an iterative pattern in each pulse cycle iteration. This only requires first cycle error data to store in memory. Unless the user change signal adjustment, this issue by RF applications with 2-D memory (I and Q as the address words), lead to deceased LUT size. In addition, methods including multi-level LUT and complex-gain-based DPD algorithms can reduce memory size. The capacity of used memory for updating error and application of distortion on input is 256. In Fig.16 and Fig.17 the used memories for each symbol are shown.

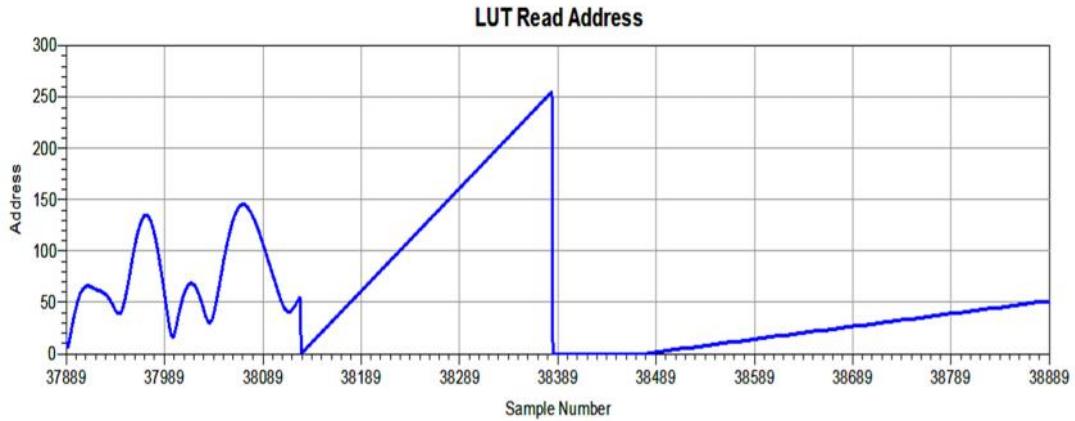


Fig. 16: Reading address of look-up table based on proposed estimated method

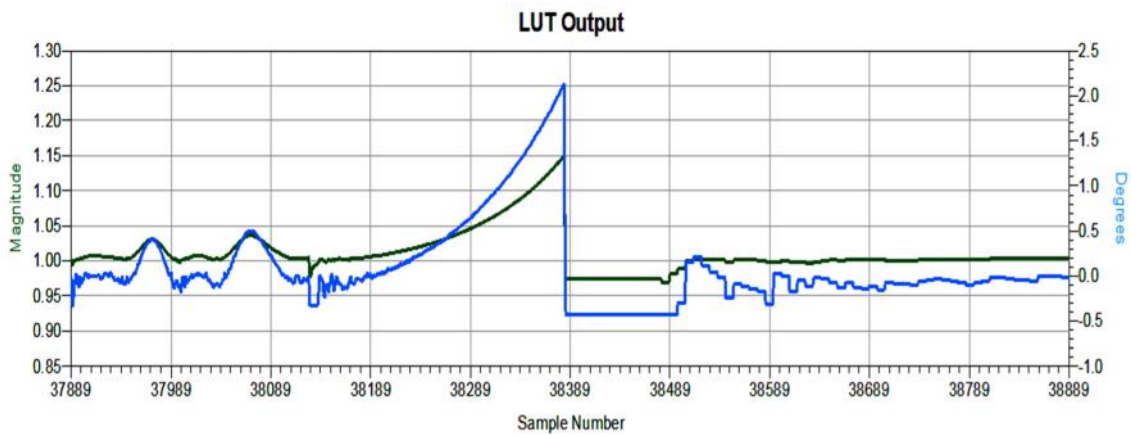


Fig. 17: Output of look-up table based on proposed estimated method

Modified Output Spectrum based on Proposed Adaptive Method

Fig. 18 and Fig. 19 shows output spectrum of amplifier before and after application of proposed digital pre-distortion (DPD) respectively. Modulator output is transmitted to the amplifier by applying of digital pre-distortion system. This, after utilization of distorted input, amplifier output is obtained without distortion of extra harmonics. As can be seen, output spectrum improves linearization of transmitted signal in the presence of pre-distortion system and decreases inappropriate harmonics.

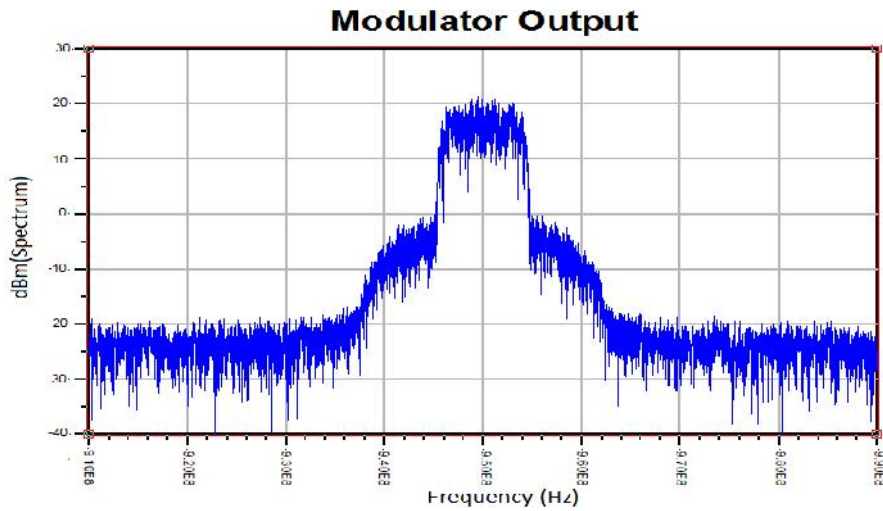


Fig. 18: Amplifier output before applying DPD system

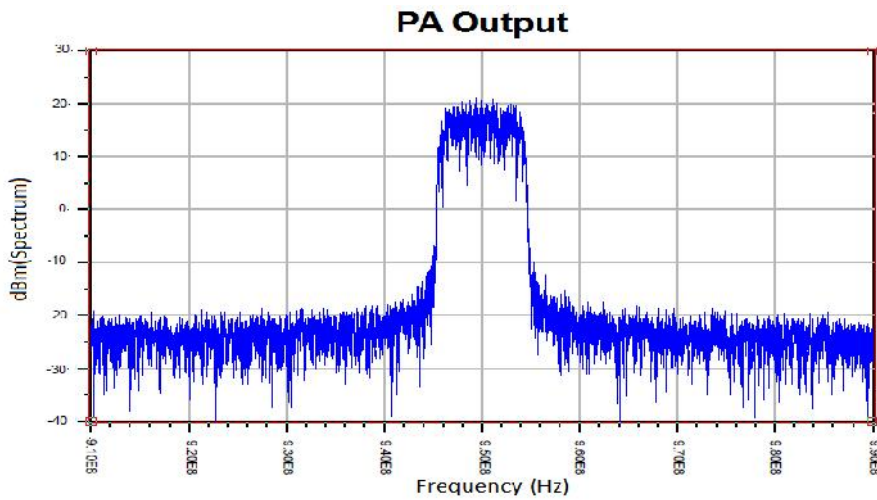


Fig. 19: Amplifier output after applying DPD system

Results of the current study compared with other references

In this section, the results obtained from combined method presented in the current paper, compared with result some of the references. In (Mrabet *et al.*, 2012), According to the results that benefited from a new hybrid method based on lock-up table and Memory-less Polynomial DPD Implementation. Results shows the additional harmonics have been weakened, but it can be observed that the harmonics have not been weakened completely in the system Fig. 20. Therefore in this paper, we achieved the desired results.

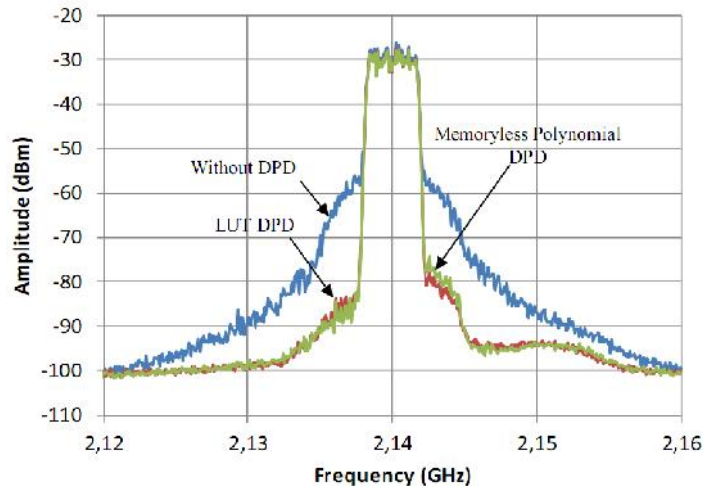


Fig. 20: 1C-WCDMA Linearization Using LUT and Memory-less Polynomial

CONCLUSION

In this paper, a new technique based on the combination of polynomial method and look-up table was proposed. This leads to as much as reduced hardware in implementation in order to have high response speed. With the aid of Agilent EESOF ADS software, the effect of power amplifier such as OFDM signal parameters, i.e., frequency spectrum and CCDF, were examined. Furthermore, in this paper, a novel linearization pre-distortion method in power amplifier based on LMS technique, as an adaptive one, was used. Consequently, in order to estimate modulator output of OFDM system, coefficients related to Look-up table by LMS technique were estimated as forward program with the least error value. The results of this method were demonstrated both in Look-up table and output signal frequency spectrum. As output spectrum improves linearization of transmitted signal and elimination of inappropriate harmonics. The results indicated high efficacy of the proposed method. ADS software was used as a simulation tool of power amplifier in OFDM system, while final results of signal were obtained by MATLAB.

APPENDIX

LMS: Least Mean Square
DPD: digital predistorter
OFDM: Orthogonal Frequency-Division Multiplexing
PAPR: Peak to Average Power Ratio
DSP: Digital Signal Processing
Lut: look-up table
RF: Radio Frequency
FPGA: Field-Programmable Gate Array
SED-DPD: slow envelope dependent digital predistorter
PA: Power Amplifier
IMD: intermodulation distortion
QAM: quadrature amplitude modulation
MS-DPD: mixed-signal digital predistorter
PLUME: Parallel-LUT-MP-EMP
2-D-MSP: Two-Dimensional Memory Selective Polynomial
GMP: generalized memory polynomial
TNTB: twin nonlinear two-box
FTNTB: Forward twin nonlinear two-box
RTNTB: reverse twin nonlinear two-box
PTNTB: parallel twin nonlinear two-box
CCDF: Complementary Cumulative Distribution Function
CDF: Cumulative Distribution Function
DAC :Digital to analog converter
ADC : Analog to Digital converter
ACPR: Adjacent Channel Power Ratio
CPD: cubic predistortion
ET: Envelope tracking
LINC: linear amplification with non-linear component
BPC: basic predistortion cell
PT: polar transmitters
MSE: mean square error

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